

Advanced Mathematics Support Programme®





• Did you use the fact that you know $8 \times 4 = 32$?

Often we use multiplication to help us do division as it is more straightforward.

- The same is true for factorising and expanding.
- It can often be easier to expand than to factorise
- So use expanding to help you factorise

I have 12 red counters and a large sheet of dotted paper. How many different rectangular arrays can I make using all 12 counters?



- An array is an arrangement of objects in rows and columns
- For this activity we will count A and B as different arrays as they have different orientations

This problem is equivalent to finding the number of rectangles with area 12 that have integer length sides, and counting 2 by 6 as different to 6 by 2



There are six arrays for 12 counters.



How many different arrays are there for:

- 7 counters?
- 15 counters?
- 25 counters?
- A prime number of counters?
- What is special about numbers with an odd number of arrays?



No of Counters	No of Arrays				
7	2	$(1 \times 7), (7 \times 1)$			
15	4	$(1 \times 15), (3 \times 5), (5 \times 3), (15 \times 1)$ $(1 \times 25), (5 \times 5), (25 \times 1)$ $(1 \times p), (p \times 1)$ (1×1)			
25	3				
Prime	2				
1	1				
Square number	Odd number				

Remember the Visual Multiplication Square from the Expanding session? How does that help?

CONTRACTOR OF STREET,							
COLUMN TWO IS NOT							
8			=				
B	B		=	 HIII			
		-	-	 -		 	







Fully factorise the following:

- **1.** 5x 30 **5.** $7a^2b + 21ab 14a$
- **2.** 9x + 6 **6.** $12x^2 + 12xy + 12y^2$

- **3.** $x^2 + 6x$ **7.** 3t(t-1) + 7(t-1)
- **4.** $6y^3 12y$ **8.** $2x(x^2 + 3) 5(x^2 + 3)$





Factorising 1



Solutions on the next slide....



Unsure about any of these? Search **Error** Factorising single brackets. Next try Skills check 2....



Fully factorise the following:

- 5. $7a^2b + 21ab 14a$
- 6. $12x^2 + 12xy + 12y^2$
- 7. 3t(t-1) + 7(t-1)

8. $2x(x^2 + 3) - 5(x^2 + 3) \rightarrow$

- = 7a(ab + 3b 2)
 - $= 12(x^2 + xy + y^2)$
 - The common factor to take out is (t 1) 3t(t - 1) + 7(t - 1)= (t - 1)(3t + 7)

The common factor to take out is $(x^2 + 3)$ $2x(x^2 + 3) - 5(x^2 + 3)$ $= (x^2 + 3)(2x - 5)$

Unsure about any of these? Search **E** Factorising single brackets. Next try Skills check 2....







Fully factorise the following:

- **1.** 7x + 28 **5.** $3x^3y 12xy^2 + 6xy$
- **2.** 14 21x **6.** $8a^3b + 6y^2b 10b$

- **3.** $y^2 8y$ **7.** 6x(x+3) + 5(x+3)
- 4. $3t^4 + 9t^2$ 8. 7y(3-2y) - 2(3-2y)

You can do this for fun - or move on if you correctly completed Skills check 1.





Factorising 2



Solutions on the next slide....





Fully factorise the following:

- 5. $3x^3y 12xy^2 + 6xy$
- 6. $8a^3b + 6y^2b 10b$

7. 6x(x+3) + 5(x+3)

8.
$$7y(3-2y) - 2(3-2y)$$

- $= 3xy(x^2 4y + 2)$
- $= 2b(4a^3 + 3y^2 5)$
- The common factor to take out is (x + 3) 6x(x + 3) + 5(x + 3)= (x + 3)(6x + 5)

The common factor to take out is (3 - 2y) 7y(3 - 2y) - 2(3 - 2y)= (3 - 2y)(7y - 2)





You are told that

ab = 245bc = 635a + c = 88

What is the value of *b*?

Hints available on the next slide





You are told that

ab = 245bc = 635a + c = 88

What is the value of *b*?

- Try adding the first two expressions together
- Now factorise
- Have another look at the question





You are told that ab = 245 bc = 635a + c = 88

What is the value of *b*?

ab + bc = 245 + 635b(a + c) = 880b(88) = 880b = 10





By considering prime factors, and without a calculator, find the square root of 27×147

Hints available on the next slide





By considering prime factors, and without a calculator, find the square root of 27×147

- Draw prime factor trees for 27 and 147 separately
- Write down 27 x 147 expressed as a product of their prime factors
- Simplify the expression
- Have another look at the question





By considering prime factors, and without a calculator, find the square root of 27×147 $27 = 3^3$ $147 = 3 \times 7^2$

Therefore $27 \times 147 = 3^3 \times 3 \times 7^2 = 3^4 \times 7^2$

 $\sqrt{27 \times 147} = \sqrt{3^4 \times 7^2} = \sqrt{3^4} \times \sqrt{7^2} = 3^2 \times 7 = 63$





Simplify $\sqrt{2y^2(x+3)^2 + 7(x+3)^2y^2}$

Hint available on the next slide





Simplify $\sqrt{2y^2(x+3)^2 + 7(x+3)^2y^2}$

Factorise first (Q7 and Q8 from Factorising 1 vill help)
Have another look at the question





Simplify
$$\sqrt{2y^2(x+3)^2 + 7(x+3)^2y^2}$$

The common factor is $(x + 3)^2$

$$\sqrt{2y^2(x+3)^2+7(x+3)^2y^2}$$

$$= \sqrt{(x+3)^2(2y^2+7y^2)}$$

$$=\sqrt{9y^2(x+3)^2}$$

=3y(x+3)



Power Puzzle



Simplify

$$\frac{4x^{2.5}-6\sqrt{x}}{2x^2-3}$$

Hints available on the next slide



Power Puzzle Hint



Simplify

$$\frac{4x^{2.5} - 6\sqrt{x}}{2x^2 - 3}$$

- Rewrite \sqrt{x} as a power of x
- What is 2.5 as a fraction?
- Factorise the numerator
- Have another look at the question





Simplify

$$\frac{4x^{2.5} - 6\sqrt{x}}{2x^2 - 3}$$

= $\frac{4x^{2.5} - 6x^{0.5}}{2x^2 - 3}$
= $\frac{2x^{0.5}(2x^2 - 3)}{2x^2 - 3}$ = $2x^{0.5} = 2\sqrt{x}$





Pick 3 different integers from 1 to 10

Place your numbers in the boxes in as many different ways as possible (i.e 6 ways) $\Box(\Box x + \Box)$

- Write down all the expressions
- Multiply them all out
- Add up all your results and simplify
- Now factorise that answer



Try again with a different set of 3 numbers

What do you notice? Can you prove it?





Factor Problem



Follow the link for hints and solutions





<u>Read</u> about the amazing properties of prime numbers. Generate large primes for yourself and find out how you can make money from solving prime number problems.



<u>Discover</u> how you can use place value and factorising to explore number tricks by attempting this nrich problem.



<u>Watch</u> this video by James Grime. See if you can work out why the trick works.



Contact the AMSP









